

## A model study of gap equation in the heavy fermion superconductors

M S Ojha<sup>1\*</sup>, G C Rout<sup>2</sup> and S N Behera<sup>3</sup>

<sup>1</sup>S. C. S. (Jr) College, Puri-752 001, Orissa, India

<sup>2</sup>Condensed Matter Physics Group, Govt Science College, Chatrapur-761 020, Orissa, India

<sup>3</sup>Institute of Physics, Sachivalaya Marg, Bhubaneswar-751 005, Orissa, India

E-mail : mojha@iopb.res.in

**Abstract** : The superconducting order parameter due to conduction electrons and the sub-lattice staggered field parameter due to the weakly delocalized *f*-electrons are calculated by Zubarev type Green function method for the heavy fermion magnetic superconductors. We solved the self-consistent mean field equations for the superconducting gap and the staggered field. The mutual influence on each other is studied by varying model parameters of the systems : the superconducting coupling ( $g_1$ ), antiferromagnetic coupling ( $g_2$ ), the hybridization ( $\nu$ ) for various temperature ranges. The results show a strong correlation between them through the suppression and enhancement of the order parameters and transition temperatures as well as a few anomalous results. This model can explain the strong coupling between magnetism and superconductivity in the  $UM_2Al_3$  and similar U-based systems.

**Keywords** : Heavy fermion superconductor, narrow band system, local moment in heavy fermions.

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### 1. Introduction

The field of heavy fermion superconductivity (HFSC) is still the subject of much research activity [1]. We discuss below some properties of the two most recent examples,  $UM_2Al_3$  ( $M = Ni ; Pd$ ) [2,3] where there exists the homogeneous coexistence between HF superconductivity and local moment magnetic (LMM) order with surprisingly large values of both  $T_c$  and  $\mu_s$ . The U-based HFSC typically show the microscopic coexistence of antiferromagnetism (AFM) and superconductivity at  $T \leq T_c \leq T_N$ . Both their SC and AFM states exhibit exotic properties. Here, we wish to mention only the discoveries of extremely small staggered moments  $\mu_s = 0.02 \mu_B$  and  $0.04 \mu_B$ , along with large commensurate ordering wave vectors for  $UPt_3$  [4] and  $URu_2Si_2$  [5] respectively. The homologs  $UM_2Al_3$  ( $M = Ni, Pd$ ) crystallize in hexagonal structure. The unit cell volume of  $UNi_2Al_3$  is smaller by 4% than that of its Pd counterpart. Consequently, the *5f*-ligand hybridization is larger in the former. Both compounds exhibit the typical signature of a Kondo lattice. The heavy fermion systems are characterized by a characteristic temperature  $T^*$  (called "Kondo lattice

temperature") above which the system shows localized character and below which the system exhibits Fermi liquid behaviour. The  $T^*$  for the Ni and Pd systems are  $\simeq 75$  K and  $\simeq 40$  K respectively. The hexagonal HFSC  $UNi_2Al_3$  ( $\gamma \simeq 120$  mJ/K<sup>2</sup>-mole,  $T_c \simeq 1$  K orders antiferromagnetically below  $T_N \simeq 4.5$  K [2]. The HFSC  $UPd_2Al_3$  ( $\gamma = 140$  mJ/K<sup>2</sup>-mole) orders antiferromagnetically with Néel temperature  $T_N = 14.5$  K [3] and the staggered magnetic moment  $\mu_s \simeq 0.85 \mu_B$  [6]. The saturated moments are larger than that for  $UPt_3$  and  $URu_2Si_2$  by one to two orders of magnitude. In particular,  $\mu_s = 0.85 \mu_B$  is as large as that for ordinary U-based magnets. It is most remarkable that such a large  $\mu_s$  coexists with HFSC below a  $T_c$ . Surprisingly large ordered moments of  $\mu_s$  are ferromagnetically aligned within the basal planes and antiferromagnetically aligned along the perpendicular directions [6]. Not only AFM but also superconductivity sets at a much higher temperature than Ni-system ( $T_c = 2$  K)

### 2. Superconducting gap

Very recently Metaki *et al* have observed a magnetic

\*Corresponding Author

excitation gap associated with superconductivity in UPd<sub>2</sub>Al<sub>3</sub> [7,8] in their neutron scattering experiment. The temperature dependence of the gap is comparable to the one of the superconducting energy gap expected from the weak coupling BCS theory. This energy gap corresponds to  $2\Delta(0) = 2.2 k_B T_c$ . It is in same order compared with the weak coupling BCS theory  $2\Delta(0) = 3.52 k_B T_c$ . A clear superconducting gap at  $2\Delta(0) = 3.8 k_B T_c$  has been observed in a study of tunneling spectroscopy of UPd<sub>2</sub>Al<sub>3</sub> thin film [9]. They also observed that the temperature dependence of this gap, which is obviously a charge gap, is very similar to the one of magnetic excitation gap. The NMR and Knight shift study [10] concludes that *d*-wave pairing is realized in UPd<sub>2</sub>Al<sub>3</sub> characterized by a line node of energy gap  $2\Delta(0) = 5.5 k_B T_c$  which is higher than the value  $2\Delta(0) = 2.2 k_B T_c$  [8] and the tunneling spectroscopy ( $2\Delta(0) = 3.8 k_B T_c$ ). They conclude saying that it may be due to the anisotropic gap. Recently Rout *et al* have considered a weak coupling BCS type pairing in the Periodic Anderson model to explain the superconducting gap anisotropy [11] and Raman spectra [12] in the non-magnetic heavy fermion superconductor.

### 3. Theoretical model

Any theoretical model which attempts to explain the observed anomaly in the UM<sub>2</sub>Al<sub>3</sub> (*M* = Ni, Pd) must take into account the simultaneous occurrence of the antiferromagnetic heavy fermion superconducting long range orders. The evidence for the origin of antiferromagnetism (AFM) point towards the more localized 5*f*-states, while the HF superconductivity in the system is due to less localized same 5*f*-electrons. In case when the AFM is due to the same itinerant 5*f*-electrons which are responsible for superconductivity, the former is more likely to be of the form of a spin density wave (SDW) arising from a Fermi surface instability [13]. However, it can be visualized that 5*f*-localized electrons can acquire some itinerant character being hybridized with the conduction electrons of the system. Then superconductivity in these systems can be thought of BCS type phonon mediated weak Cooper pairing in the conduction electrons which exhibits anisotropic *d*-wave type superconductivity [11,12,14,]. In the model presented below, however, the AFM is attributed to a staggered sub-lattice magnetization arising from the 5*f*-delocalized electrons which coexists with superconductivity arising from the conduction electrons. The aim of the present calculation is to assume a simple model in order to investigate the effect of the SC and the AFM coupling constants on the coexistence of AFM and SC in the

system. The Hamiltonian of the system is described by

$$\mathcal{H} = \mathcal{H}_c + \mathcal{H}_f^1 + \mathcal{H}_f^2 + \mathcal{H}_h + \mathcal{H}_v + \mathcal{H}_s \quad (1)$$

The uranium(U) site is divided into two sub-lattices 1 and 2 with corresponding creation operators  $c_{1,i,\sigma}^\dagger$  and  $c_{2,i,\sigma}^\dagger$  respectively of the conduction electrons. The hopping of the conduction electrons between the nearest neighbour sites of the two sub-lattices is described by

$$\mathcal{H}_c = - \sum_{i,j,\sigma} t_{ij} (c_{1,i,\sigma}^\dagger c_{2,j,\sigma} + h.c.) \quad (2)$$

The Fourier transformed form of  $\mathcal{H}_c$  is

$$\mathcal{H}_c = \sum_{k,\sigma} \epsilon_k (c_{1,k,\sigma}^\dagger c_{2,k,\sigma} + c_{2,k,\sigma}^\dagger c_{1,k,\sigma}) \quad (3)$$

where  $c_{1,k,\sigma}^\dagger$  and  $c_{2,k,\sigma}^\dagger$  are the creation operators of electrons belonging to the two sub-lattices 1 and 2 respectively with momentum *k* and spin  $\sigma$ . The dispersion of the charge carriers is  $\epsilon_k$  which is the Fourier transform of the nearest neighbour hopping matrix element  $t_{ij}$ . Similarly the Hamiltonian  $\mathcal{H}_f$  describes the intra *f*-electrons in the localized levels corresponding to the flat band,

$$\mathcal{H}_f^1 = \epsilon_f \sum_{k,\sigma} (f_{1,k,\sigma}^\dagger f_{1,k,\sigma} + f_{2,k,\sigma}^\dagger f_{2,k,\sigma}) \quad (4)$$

where  $f_{i,k,\sigma}^\dagger$  ( $f_{i,k,\sigma}$ ) are the creation (annihilation) operators of the localized electrons in the sub-lattice *i* ( $\equiv 1,2$ ) and  $\epsilon_f$  is the dispersionless and the renormalized energy of the localized levels. For simplicity of the calculation the renormalized  $\epsilon_f$  is assumed to lie exactly on the Fermi level  $\epsilon_F = 0$ . The intersite *f*-electron hopping in real space is described by the Hamiltonian  $\mathcal{H}_f^2$  as

$$\mathcal{H}_f^2 = - \sum_{i,j,\sigma} e_{ij} (f_{1,i,\sigma}^\dagger f_{2,j,\sigma} + h.c.) \quad (5)$$

where  $f_{1,i,\sigma}^\dagger$  and  $f_{2,j,\sigma}^\dagger$  are the creation operators of the *f*-electrons at two different sub-lattices 1 and 2 respectively with spin  $\sigma$ . The  $e_{ij}$  is the nearest neighbour *f*-electron hopping matrix element. The Fourier transformed *f*-electron hopping Hamiltonian is given by

$$\mathcal{H}_f^2 = \sum_{k,\sigma} E_0(k) (f_{1,k,\sigma}^\dagger f_{2,k,\sigma} + f_{2,k,\sigma}^\dagger f_{1,k,\sigma}) \quad (6)$$

where  $E_0(k)$  gives the narrow dispersion of the *f*-electron band. The sub-lattice magnetization due to the *f*-electron lattice arise from the Heisenberg exchange interaction between the magnetic moments at neighbouring sites. Within

the mean field approximation the Hamiltonian  $\mathcal{H}_h$  for the staggered sub-lattice magnetization can be written as

$$\mathcal{H}_h = (h/2) \sum_{k,\sigma} (f_{1,k,\sigma}^\dagger f_{1,k,\sigma} - f_{2,k,\sigma}^\dagger f_{2,k,\sigma}), \quad (7)$$

where  $h$  is the strength of the sub-lattice magnetization which stimulates AFM correlation of the  $f$ -electrons. The Hamiltonian  $\mathcal{H}_v$  describing the hybridization is given by

$$\mathcal{H}_v = V \sum_{k,\sigma} (c_{1,k,\sigma}^\dagger f_{1,k,\sigma} + c_{2,k,\sigma}^\dagger f_{2,k,\sigma} + h.c.), \quad (8)$$

where the strength of hybridization ( $V$ ) is wave vector and spin independent. It should be noted that only the on-site hybridization is induced *i.e.* the localized electron belonging to the sub-lattice 1 hybridizes with the conduction electrons of that sub-lattice alone, and so on. The strong onsite Coulomb correlation in these systems which mainly accounts for its heavy fermion behaviour is given by

$$\mathcal{H}_I = U_f \sum_{i,j} (n_{1,i,\uparrow}^f n_{1,i,\downarrow}^f + n_{2,i,\uparrow}^f n_{2,i,\downarrow}^f), \quad (9)$$

where  $U_f$  is the Coulomb correlation energy of the  $f$ -electrons at sub-lattices 1 and 2. The heavy fermion superconductors  $\text{UM}_2\text{Al}_3$  ( $M = \text{Pd, Ni}$ ) are unconventional anisotropic superconductors, probably  $d$ -wave. In addition, there is some evidence that the superconductivity is mediated by antiferromagnetic spin-fluctuations [15]. However, we consider the mean field BCS Hamiltonian describing phonon mediated superconductivity is given by

$$\mathcal{H}_s = -\Delta \sum (c_{1,k\uparrow}^\dagger c_{1,-k\downarrow}^\dagger + c_{2,k\uparrow}^\dagger c_{2,-k\downarrow}^\dagger + h.c.), \quad (10)$$

where

$$\Delta_k = -\sum \tilde{V}_k (<c_{1k\uparrow}^\dagger c_{1-k\downarrow}^\dagger> + <c_{2k\uparrow}^\dagger c_{2-k\downarrow}^\dagger>), \quad (11)$$

where only intra sub-lattice pairing is assumed and  $\Delta$  is the wave vector independent  $s$ -wave superconducting order parameter. It may be noted that the total Hamiltonian of the system is a mean field one and hence can be solved exactly either by appropriate diagonalization using the Bogoliubov transformation or by writing the equations of motion for the single particle Greens function [16]. The later procedure has been followed to solve for the Greens functions and to calculate the appropriate single particle correlation functions which in turn determines the order parameters corresponding to the AFM and SC long range orders.

#### 4. Calculation of electron Green's functions

We calculate the one electron Green functions using the Hamiltonian  $\mathcal{H}$  given in eq. (1) for the superconducting state of the HF system. The double time electron Green functions of Zubarev type [16] are calculated by equations of motion method. The Green functions  $A_i(k, \omega)$ ,  $B_i(k, \omega)$ ,  $E_i(k, \omega)$ ,  $F_i(k, \omega)$ ,  $G_i(k, \omega)$ , and  $H_i(k, \omega)$ , (with  $i = 1-8$ ) are the coupled set which are involved in the calculation. Finally the SC gap and magnetic order parameters are calculated by using the Green's functions defined below in eq. (12).

$$A_2(k, \omega) = \langle\langle c_{1,-k\downarrow}^\dagger; c_{1,k\uparrow}^\dagger \rangle\rangle_\omega,$$

$$B_2(k, \omega) = \langle\langle c_{2,-k\downarrow}^\dagger; c_{2,k\uparrow}^\dagger \rangle\rangle_\omega,$$

$$E_1(k, \omega) = \langle\langle f_{1,k\uparrow}; f_{1,k\uparrow}^\dagger \rangle\rangle_\omega,$$

$$F_1(k, \omega) = \langle\langle f_{1,k\downarrow}; f_{1,k\downarrow}^\dagger \rangle\rangle_\omega,$$

$$G_1(k, \omega) = \langle\langle f_{2,k\uparrow}; f_{2,k\uparrow}^\dagger \rangle\rangle_\omega,$$

$$H_1(k, \omega) = \langle\langle f_{2,k\downarrow}; f_{2,k\downarrow}^\dagger \rangle\rangle_\omega. \quad (12)$$

The coupled equations are solved to find out the Green's functions defined in eq. (12) (dropping the functional dependences *i.e.*  $(k, \omega)$  for simplicity).

$$A_2 = \frac{1}{4\pi} \frac{(\omega - \Delta)(\omega^2 - \tilde{\epsilon}_f^2) - V^2(\omega - h/2)}{|D_1(\omega)|}$$

$$- \frac{(\omega + \Delta)(\omega^2 - \tilde{\epsilon}_f^2) - V^2(\omega - h/2)}{|D_2(\omega)|} \quad (13)$$

where

$$\begin{aligned} |D_{1,2}(\omega)| &= (\omega^2 - E_k^2)(\omega^2 - \tilde{\epsilon}_f^2) \\ &\quad - 2V^2\{\omega^2 \mp \Delta h/2 + E_0(k) \epsilon_k\} + V^4 \\ &= \omega^4 - R\omega^2 + S_{1,2} \end{aligned} \quad (14)$$

with

$$\begin{aligned} R &= E_k^2 + \tilde{\epsilon}_f^2 + 2V^2, \\ S_{1,2} &= E_k^2 \tilde{\epsilon}_f^2 \pm \Delta h V^2 - 2\epsilon_k E_0(k) V^2 + V^4, \end{aligned}$$

$$E_k^2 = \epsilon^2 + \Delta^2, \quad (15)$$

$$\tilde{\epsilon}_f^2 = E_0^2(k) + \hbar^2/4.$$

The poles of the Green's functions given in eqs. (13) give eight quasi-particle energy bands  $\pm\omega_i$  ( $i = 1$  to 4).

### 5. Expressions for SC and AFM gaps

We have used here a phonon mediated B.C.S. type of Cooper pairing between conduction electrons. The expression for energy gap parameter ( $\Delta$ ) for intra-sublattice pairing can be calculated from the Green functions  $A_2(k, \omega)$  and  $B_2(k, \omega)$  given in eq. (12) respectively. The superconducting gap is defined as

$$\Delta_k = -\sum \tilde{V}_k [c_{1,k\uparrow}^\dagger c_{1,-k\downarrow}^\dagger c_{2,k\uparrow}^\dagger c_{2,-k\downarrow}^\dagger], \quad (16)$$

$\tilde{V}_k$  being the strength of the attractive interaction between the two electrons mediated by the phonons. We have a limitation on the  $k$ -sum owing to the restriction that the attractive interaction is only effective with energy  $|\epsilon_1 - \epsilon_2| < \omega_D$ . Here, the attractive interactions between two carriers are  $\epsilon_1$  and  $\epsilon_2$  to form the Cooper pairs and  $\omega_D$  is the Debye frequency. Further, we adopt the following simplified form for the interaction potential  $\tilde{V}_k$  in the ordinary isotropic weak coupling limit. Here  $\tilde{V}_k = -V_0$ , if  $|\epsilon_1 - \epsilon_2| < \omega_D$ ,  $\tilde{V}_k = 0$ , otherwise. In this approximation we assume that the gap parameter is independent of  $k$ . The superconductivity in UPd<sub>2</sub>Al<sub>3</sub> is believed to be anisotropic and unconventional. However, we can observe some important features of interplay of SC and AFM from this simplified eq. (16). The final expression for superconducting energy gap is

$$\Delta(T) = \frac{V_0 N(0)}{4} \int_{-\omega_D}^{\omega_D} d\epsilon_k \left[ \frac{F_{11} - F_{21}}{\omega_1^2 - \omega_2^2} + \frac{F_{31} - F_{41}}{\omega_3^2 - \omega_4^2} \right], \quad (17)$$

where

$$F_{i1} = K_i \tanh(\beta\omega_i/2), \quad (18)$$

$$K_1 = \frac{2\Delta(\omega_1^2 - \tilde{\epsilon}_f^2) - \hbar V^2}{\omega_1},$$

$$K_2 = \frac{2\Delta(\omega_2^2 - \tilde{\epsilon}_f^2) - \hbar V^2}{\omega_2},$$

$$K_3 = \frac{2\Delta(\omega_3^2 - \tilde{\epsilon}_f^2) + \hbar V^2}{\omega_3},$$

$$K_4 = \frac{2\Delta(\omega_4^2 - \tilde{\epsilon}_f^2) + \hbar V^2}{\omega_4} \quad (19)$$

with  $i = 1-4$ .  $N(0)$  is the density of states of the conduction band at the Fermi level. We replace  $\sum_k$  by  $\int N(0) d\epsilon_k$  with integration limit from  $-\omega_D$  to  $+\omega_D$ . We have introduced the staggered magnetic field on uranium sites to break the spin symmetry in the  $f$ -electrons. The AFM order parameter  $h$  in  $f$ -electrons is defined as

$$h = -\frac{1}{2} g_L \mu_B \sum_{k,\sigma} \sigma [ \langle f_{1,k,\sigma}^\dagger f_{1,k,\sigma} \rangle - \langle f_{2,k,\sigma}^\dagger f_{2,k,\sigma} \rangle ], \quad (20)$$

where  $g_L$  and  $\mu_B$  are Lande  $g$ -factor and Bohr magneton respectively. The correlation functions  $\langle f_{1,k,\uparrow}^\dagger f_{1,k,\uparrow} \rangle$  and  $\langle f_{1,k,\downarrow}^\dagger f_{1,k,\downarrow} \rangle$  are calculated from the Green functions  $E_1(k, \omega)$  and  $F_1(k, \omega)$ . Similarly the correlation functions  $\langle f_{2,k,\uparrow}^\dagger f_{2,k,\uparrow} \rangle$  and  $\langle f_{2,k,\downarrow}^\dagger f_{2,k,\downarrow} \rangle$  are calculated from the Green functions  $G_1(k, \omega)$  and  $H_1(k, \omega)$ . The final expression for the staggered magnetic field is given by

$$h = \frac{g_2}{4} \int_{-W/2}^{+W/2} d\epsilon_k \left[ \frac{E_{11} - E_{21}}{\omega_1^2 - \omega_2^2} + \frac{E_{31} - E_{41}}{\omega_3^2 - \omega_4^2} \right], \quad (21)$$

where

$$E_{i1} = E_i \tanh(\beta\omega_i/2); \quad (22)$$

$$E_1 = \frac{\hbar(\omega_1^2 - E_k^2) - 2\Delta V^2}{\omega_1},$$

$$E_2 = \frac{\hbar(\omega_2^2 - E_k^2) - 2\Delta V^2}{\omega_2},$$

$$E_3 = \frac{\hbar(\omega_3^2 - E_k^2) + 2\Delta V^2}{\omega_3},$$

$$E_4 = \frac{\hbar(\omega_4^2 - E_k^2) + 2\Delta V^2}{\omega_4} \quad (23)$$

with  $i = 1-4$ .  $W$  is the band width of the  $f$ -electron and  $g_2 = g_L \mu_B N_f(0)$ . The  $\sum_k \rightarrow \int N_f(0) d\epsilon_k$  where  $N_f(0)$  is the density of states of the  $f$ -electron band near the Fermi level. The eqs. (17) and (21) form a coupled set of equations for the two order parameters  $\Delta(T)$  and  $h(T)$  which are to be determined self consistently to study their temperature

dependence and mutual interplay. All the quantities entering in eqs. (17) and (21) are made dimensionless by dividing them by Debye energy  $\omega_D$ . Thus, the dimensionless order parameters are defined as  $\Delta(T)/\omega_D = z$  and  $h/\omega_D = h$ , the variables as  $\epsilon_k/\omega_D = x$ ,  $k_B T/\omega_D = t$ ,  $V/\omega_D = V$ . The dimensionless coupling constants are  $N(0)V_0 = g_1$  and  $g_L \mu_B N_f(0) = g_2$ .

## 6. Results and discussion

The interplay of superconductivity (SC) and antiferromagnetism (AFM) in the heavy fermion (HF) systems  $\text{UM}_2\text{Al}_3$  can be studied by varying different model parameters of the electronic sub-system. These parameters are the SC gap  $z$ , AFM gap  $h$ , SC coupling constant  $g_1$ , AFM coupling constant  $g_2$ , the hybridization parameter ( $\nu$ ) between the conduction and  $f$ -electrons, temperature  $t$ . The position of  $f$ -electron energy level assumed to lie on the fermi level  $\epsilon_F$  under the half filling band situation.

The temperature variation of SC gap  $z$ , AFM gap  $h$  are shown in Figure 1 before interplay. They are calculated numerically and self-consistently with an accuracy of  $10^{-4}$ . The SC plot gives a SC gap  $z(t=0) = 0.0077$  and transition temperature  $t_c = 0.0025$  corresponding to universal constant  $\Delta(0)/k_B T = 3.08$  as against BCS value 1.76. The corresponding SC coupling constant  $g_1 = 0.09916$ . Similarly the AFM plot gives a Néel temperature  $t_N = 0.0014$  corresponding to an AFM coupling  $g_2 = 0.18822$ . These parameters are fixed for  $t_c > t_N$  before interplay between SC and AFM.

When these two order parameters interplay the self-consistent plot is shown in Figure 2. As compared to their values before interplay it is observed that the SC transi-

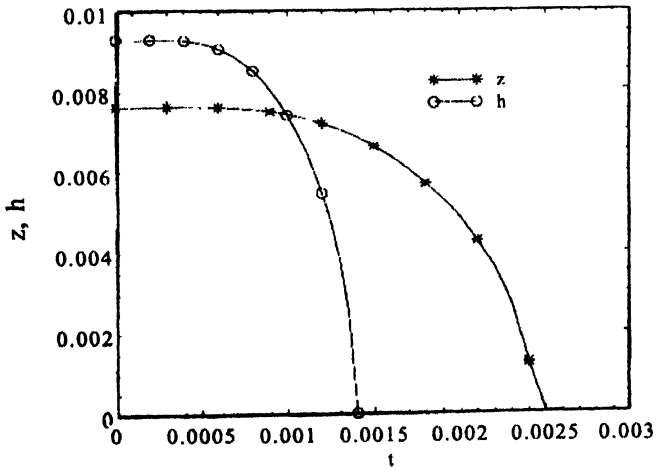


Figure 1. Individual plots of  $z$  vs  $t$  for  $h = 0$ ,  $\nu = 0.02$ ,  $g_1 = 0.09916$  and plot of  $h$  vs  $t$  for  $z = 0$ ,  $\nu = 0.02$  and  $g_2 = 0.18822$ .

tion temperature  $t_c$  is suppressed considerably by AFM to nearly one-third of its value. The SC gap also suppressed considerably to nearly one-third of its value giving rise to

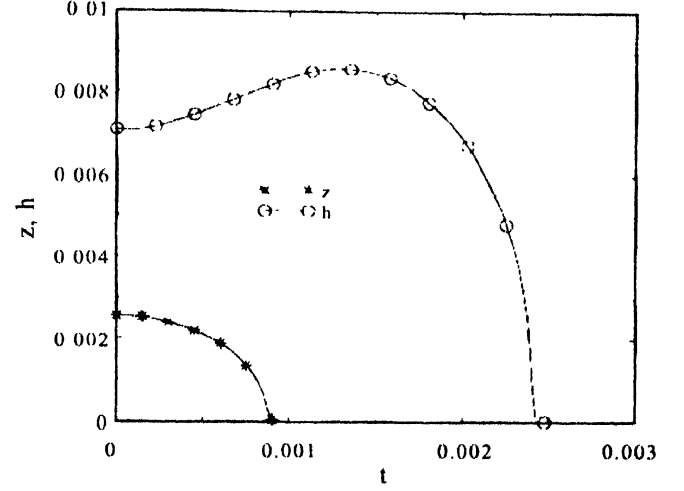


Figure 2. Self consistent plots of  $z$  vs  $t$  and  $h$  vs  $t$  with fixed values of  $\nu = 0.02$ ,  $g_1 = 0.09916$  and  $g_2 = 0.18822$ .

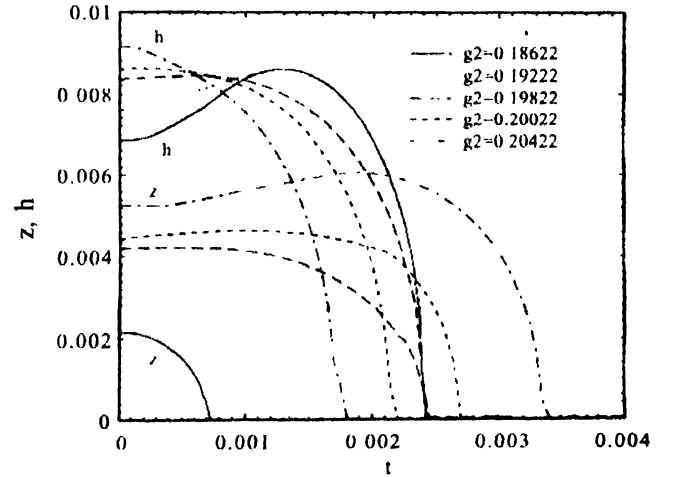


Figure 3. Self consistent plots of  $z$  vs  $t$  and  $h$  vs  $t$  with fixed values of  $\nu = 0.02$  and  $g_1 = 0.09916$  for different values of  $g_2 = 0.18622, 0.19222, 0.19822, 0.20022$  and  $0.20422$ .

the BCS universal value  $\Delta(0)/k_B T \approx 2.94$ . But the AFM Néel temperature  $t_N$  is enhanced to double its value by superconductivity. The AFM staggered field  $h(T=0)$  is suppressed a little from  $h(0) = 0.0094$  to  $0.0075$ . Again the  $t_c$  and  $t_N$  values are nearly in conformity with experimental observation : i.e.  $t_N > t_c$ . The experiment gives  $T_N = 4.5$  K and  $T_c = 1$  K for  $\text{UNi}_2\text{Al}_3$  system [2], and  $T_N = 14.5$  K and  $T_c = 2$  K for  $\text{UPd}_2\text{Al}_3$  [3]. Neutron scattering experiments [7,8] shows that the observed magnetic peak intensities increase continuously from the Néel temperature  $T_N$  down

to  $T_c$ . Below  $T_c$ , the magnetic peak intensities turn to decrease with decreasing the sample temperature. They confirmed that the suppression of the magnetic intensities is due to superconductivity. This behaviour can be understood in terms of the coupling between magnetic and superconducting order parameter as given in the present model. It is concluded that the coupling of the magnetic and superconducting order parameters would be a characteristic feature in the heavy fermion superconductors.

The effect of the AFM coupling  $g_2$  on the SC gap (see lower panel) and the AFM gap (see upper panel) is shown in Figure 3. It unambiguously displays the strong correlation between the superconductivity and antiferromagnetism. The increase of the AFM coupling  $g_2$  enhances the SC order parameter (lower panel) throughout the temperature range and the SC transition temperature (from  $t_c = 0.00085$  to  $0.0035$  lower panel). It is interesting to note that the increase of  $g_2$  from  $0.18622$  to  $0.20422$  reduces the BCS universal constant from  $\Delta(0)/k_B T = 2.94$  to a value of  $\approx 2.08$  indicating a considerable suppression of the SC gap at low temperature where the AFM order (see upper panel) is stronger than the SC gap. The effect of the AFM coupling  $g_2$  on its own staggered field is still more interesting. It is well known that the AFM coupling  $g_2$  should enhance the magnitude of the staggered field  $h$  as well as the Néel temperature  $t_N$ . However the interplay between the SC and AFM exhibits some anomalies in the staggered field  $h$  (upper panel) when the AFM coupling  $g_2$  increases gradually. For lower values of the AFM coupling ( $g_2 < 0.19222$ ), the Néel temperature remains unaltered indicating its sharpness and robustness. However the staggered field strength  $h$  increases at low temperatures with increase of the AFM coupling (which is commonly anticipated). In this low temperature range ( $t < 0.0015$ ), both the order parameters  $z$  and  $h$  are enhanced with increase of the AFM coupling  $g_2$  even though suppression in the low temperature range is obvious in both the order parameters

due to their mutual interaction. In conclusion, we can say that present model can explain the strong coupling between the magnetism and superconductivity.

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